

EXPLORATION OF THE POTENTIAL PERFORMANCE
OF DIODE LASER PUMPED GAS CELL
ATOMIC FREQUENCY STANDARDS

J. C. Camparo and R. P. Frueholz
Chemistry and Physics Laboratory
The Aerospace Corporation
P. O. Box 92957
Los Angeles, CA 90009

ABSTRACT

Recently, there has been considerable interest in the use of single-mode diode lasers in atomic frequency standards. In the present paper theoretical calculations are performed in order to quantify the expected performance improvement upon incorporation of diode lasers in rubidium gas cell atomic frequency standards. We assume that clock signal shot noise, the diode laser's quantum noise and diode laser frequency locking noise all contribute to the atomic frequency standard's stability. Our results indicate that white noise Allan variances of $\sim 6 \times 10^{-15} / \sqrt{\tau}$ are possible if enhanced cavity Q diode lasers are employed, whereas for presently available commercial diode lasers we predict white noise Allan variances of $3 \times 10^{-14} / \sqrt{\tau}$. These variances represent a 2-3 orders of magnitude improvement in frequency stability over that currently obtained with rubidium gas cell atomic clocks.

INTRODUCTION

Recently, there has been considerable interest in and speculation on the use of single-mode diode lasers for optical pumping in atomic frequency standards. In particular, current efforts are primarily focused on the cesium beam frequency standard,¹ where atomic state preparation by diode laser optical pumping and atomic state detection by diode laser induced fluorescence are envisaged as replacing the traditional A and B magnets of atomic beam standards. The impetus for this activity is the many possible advantages of optical state preparation and detection, for example greater signal to noise ratios,² and recent theoretical and experimental work would indicate that these expectations are well founded.^{3,4} However, in addition to the cesium beam frequency standard work there has also been a growing interest in the area of diode laser optical pumping in rubidium gas cell frequency standards,⁵ where it is anticipated that diode laser optical pumping will both improve the signal to noise ratio and drastically reduce light shift effects.⁶ Unfortunately, in contrast to the cesium beam studies, to date there have been no theoretical calculations to support these expectations or to provide insights into the choice of the optimal optical pumping conditions.

Report Documentation Page			<i>Form Approved OMB No. 0704-0188</i>					
<p>Public reporting burden for the collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington VA 22202-4302. Respondents should be aware that notwithstanding any other provision of law, no person shall be subject to a penalty for failing to comply with a collection of information if it does not display a currently valid OMB control number.</p>								
1. REPORT DATE DEC 1985	2. REPORT TYPE	3. DATES COVERED 00-00-1985 to 00-00-1985						
4. TITLE AND SUBTITLE Exploration of the Potential Performance of Diode Laser Pumped Gas Cell Atomic Frequency Standards			5a. CONTRACT NUMBER					
			5b. GRANT NUMBER					
			5c. PROGRAM ELEMENT NUMBER					
6. AUTHOR(S)			5d. PROJECT NUMBER					
			5e. TASK NUMBER					
			5f. WORK UNIT NUMBER					
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) The Aerospace Corporation, Chemistry and Physics Laboratory, PO Box 92957, Los Angeles, CA, 90009			8. PERFORMING ORGANIZATION REPORT NUMBER					
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)			10. SPONSOR/MONITOR'S ACRONYM(S)					
			11. SPONSOR/MONITOR'S REPORT NUMBER(S)					
12. DISTRIBUTION/AVAILABILITY STATEMENT Approved for public release; distribution unlimited								
13. SUPPLEMENTARY NOTES Proceedings of the Seventeenth Annual Precise Time and Time Interval (PTTI) Applications and Planning Meeting, Washington, DC, 3-5 Dec 1985								
14. ABSTRACT see report								
15. SUBJECT TERMS								
16. SECURITY CLASSIFICATION OF: <table border="1" style="display: inline-table; vertical-align: middle;"> <tr> <td style="padding: 2px;">a. REPORT unclassified</td> <td style="padding: 2px;">b. ABSTRACT unclassified</td> <td style="padding: 2px;">c. THIS PAGE unclassified</td> </tr> </table>			a. REPORT unclassified	b. ABSTRACT unclassified	c. THIS PAGE unclassified	17. LIMITATION OF ABSTRACT Same as Report (SAR)	18. NUMBER OF PAGES 16	19a. NAME OF RESPONSIBLE PERSON
a. REPORT unclassified	b. ABSTRACT unclassified	c. THIS PAGE unclassified						

In order to remedy this situation the present series of theoretical calculations were undertaken. In particular, we consider a rubidium gas cell atomic frequency standard operating in its traditional configuration (i.e., cw optical pumping), except that the typical rf discharge lamp used for optical pumping is replaced by a single-mode diode laser tuned to the $5^2P_{3/2}(F=0,1,2,3) - 5^2S_{1/2}(F=2)$ optical absorption resonance of Rb⁸⁷. Furthermore, we assume that there is no filter cell, and that the resonance cell contains pure Rb⁸⁷. The calculations are performed in such a way that for a particular incident diode laser intensity we calculate the resonance cell temperature and peak microwave Rabi frequency that minimize the shot noise limited Allan variance as well as the minimum Allan variance itself. Additionally, we estimate the effect of frequency noise for a frequency stabilized diode laser on the frequency standard's performance. This noise is transferred to the atomic standard via the light shift effect,⁷ and as will be shown below it limits the ultimate frequency standard stability.

OVERVIEW OF THE GAS CELL FREQUENCY STANDARD MODEL

In a previous publication we introduced and validated a non-empirical model of the gas cell atomic frequency standard.⁸ In brief, this model considers the relevant gas phase physics as occurring on two different scales. On the microscopic scale the 0-0 hyperfine transition lineshape of an arbitrary alkali atom of half-integer nuclear spin is determined by the generalized Vanier theory of alkali atom hyperfine optical pumping.^{9,10} Among other parameters this theory considers the dependence of the hyperfine lineshape on optical pumping light intensity and microwave Rabi frequency. However, because the buffer gas pressure in a gas cell standard effectively freezes the alkali atoms in place on time scales of the order of a Rabi period,¹¹ and because the alkali vapor is not necessarily optically thin, these two parameters, and hence the microscopic lineshape, vary from atom to atom within the vapor. Furthermore, as a result of diffusion to the resonance cell walls, where the atoms immediately depolarize on impact, there is a spatial distribution of hyperfine polarization $\langle \vec{I} \cdot \vec{S} \rangle$. In some sense this spatial distribution of $\langle \vec{I} \cdot \vec{S} \rangle$ can be imagined as being superimposed on the microscopic physics. Thus, there is a macroscopic scale of physics in the problem which is related to both the spatial variation of optical pumping light intensity and microwave Rabi frequency, and the spatial distribution of $\langle \vec{I} \cdot \vec{S} \rangle$ due to diffusion to the resonance cell walls.

In order to treat this macroscopic scale of physics in a reasonably lucid manner, the problem was reduced to one dimension, so that only the longitudinal variation of the optical pumping rate and microwave field strength was considered. This is reasonable because the microwave field can be made uniform in the transverse dimension by dielectrically loading the cavity, and because the laser intensity can easily be made uniform

across the face of the resonance cell. The microwave Rabi frequency distribution along the axial dimension was determined by the microwave cavity mode, assuming that the atomic resonance cell filled the microwave cavity. The axial variation of the optical pumping light intensity was determined by computing a "global" optical pumping parameter ζ in a self-consistent manner. In essence, this global optical pumping parameter determined the fractional population in the optically absorbing hyperfine multiplet, and thus the optical depth of the vapor as a result of optical pumping. Since we assumed that the alkali atoms were effectively frozen in place in the resonance cell, the first order change in transmitted light intensity as a function of microwave Rabi frequency for a wedge of vapor of thickness dz only depended on the local values of the optical pumping light intensity and microwave Rabi frequency. In order to include the effect of axial diffusion this first order macroscopic solution was multiplied by the envelope function $f(z)$, which described the axial distribution of hyperfine polarization in an optically thin vapor. When considering optical pumping with lamps, where the relative optical pumping rates are typically low, it is fair to approximate $f(z)$ by Minguzzi et al.'s first order diffusion mode:¹²

$$f(z) = \sin(\pi z/L) , \quad (1)$$

where L is the length of the resonance cell. However, as discussed by Franz,¹³ when the optical pumping rate increases this approximation is no longer valid; this point will be considered in more detail below.

THE LASER PUMPED GAS CELL CLOCK

Diffusion

In order to determine the envelope function $f(z)$ for the potentially high optical pumping rates associated with the use of a diode laser, we consider the thin vapor optical pumping rate equation for a two level atom subject to diffusion in only one dimension:

$$\frac{dP}{dt} = D \frac{d^2P}{dz^2} - \left(\gamma_1 + \frac{R}{2} \right) P + \frac{R}{2} \quad (2)$$

where P is defined as the normalized population difference between the two levels (i.e., $P = (n_1 - n_2)/(n_1 + n_2)$, where n_i is the number density of atoms in the level i); and γ_1 , R and D are, respectively, the longitudinal collisional relaxation rate, the photon absorption rate (only one of the two levels is assumed to interact with the light) and the diffusion coefficient. In steady-state the solution of Eq. (2) is

$$P(z) = \left(\frac{R}{R + 2\gamma_1} \right) [1 - \exp(-\alpha z)] \left\{ 1 - \exp\left(-\frac{\alpha(L-z)}{2}\right) \left[\frac{\cosh(\alpha z/2)}{\cosh(\alpha L/2)} \right] \right\} \quad (3)$$

where

$$\alpha \equiv \sqrt{\left(\gamma_1 + \frac{R}{2}\right)/D} \quad (4)$$

Normalizing $P(z)$ to its peak value we obtain the form of $f(z)$ for arbitrary optical pumping rates:

$$f(z) = \frac{[1 - \exp(-\alpha z)] [\exp(\alpha L) - \exp(\alpha z)]}{[1 - \exp(-\alpha L/2)] [\exp(\alpha L) - \exp(\alpha L/2)]} \quad (5)$$

This envelope function is shown in Fig. 1 for several values of the relative photon absorption rate for the case of negligible collisional relaxation (i.e., $\gamma_1 = 0$). It should be noted that as the photon absorption rate increases, the envelope function becomes nearly constant. Thus, the contribution of atoms closer to the resonance cell walls becomes progressively more important, implying that at high photon absorption rates the vapor is more efficiently exploited. Note also that even at relatively low photon absorption rates the vapor is more effectively exploited than the first order diffusion mode approximation would lead one to expect. This phenomenon is shown more clearly in Fig. 2, where the full width at half maximum of the envelope function is plotted as a function of the relative photon absorption rate. From this figure it is clear that once the photon absorption rate is roughly an order of magnitude greater than the rate of diffusion to the resonance cell walls (i.e., D/L^2), the first order diffusion mode approximation to $f(z)$ is no longer valid.

Laser Stability

In any attempt to realistically model the performance of a laser pumped gas cell atomic frequency standard the frequency and intensity stability of the laser must be considered, since this is directly transferred to the frequency standard's stability via the light shift effect.¹⁴ In order to estimate the significance of laser stability on the standard's performance, we assume that the laser intensity and frequency noise are uncorrelated, so that

$$\delta f = \frac{\partial f}{\partial v} \delta v + \frac{\partial f}{\partial I} \delta I \quad (6)$$

where f , v and I correspond, respectively, to the microwave hyperfine transition frequency, the optical laser frequency and the laser intensity. Furthermore, we imagine that in any practical device the laser frequency will be actively stabilized to the center of the atomic absorption line, so that we take $\partial f / \partial I = 0$. Thus, the frequency fluctuations of the atomic standard only depend on the sensitivity of the hyperfine transition frequency to the laser frequency fluctuations, $\partial f / \partial v$, and the magnitude of the laser's frequency fluctuations, δv . Obviously, it is important to minimize both of these quantities for the best performance.

As discussed by Mathur et al.¹⁴ one can minimize $\partial f / \partial v$ by increasing the buffer gas pressure in the resonance cell. However, one cannot increase the buffer gas pressure without bound; because once the pressure broadening of the optical absorption line exceeds the ground state hyperfine splitting, depopulation pumping cannot create a population imbalance between the two ground state hyperfine multiplets. Since pressure broadening rates are typically on the order of 10 MHz/torr,¹⁵ and since the Rb⁸⁷ ground state hyperfine splitting is ~7 GHz, we estimated that roughly 100 torr of buffer gas (our calculation assumes nitrogen) was the limit on the maximum buffer gas pressure.

Recently, Ohtsu et al.¹⁶ estimated the ultimate frequency stability of presently available diode lasers due to quantum noise. Basically, the ultimate frequency stability of a diode laser is related to quantum noise via three different mechanisms. Fundamentally, there is the direct quantum noise due to the phase noise associated with spontaneous emission. Additionally, however, because the index of refraction of the diode laser depends on the carrier density, the relaxation oscillations of the carrier density following a spontaneous emission event alter the phase of the entire laser field.¹⁷ Furthermore, since the carrier density relates to ohmic heating, and since the index of refraction of the semiconductor material also depends on temperature, there is an additional fluctuation in the phase of the laser field following a spontaneous emission event. Together, these processes yield a white noise Allan variance for the laser frequency stability in CSP diode lasers $\sigma_y^L(\tau)$ of $9.02 \times 10^{-12} / \sqrt{\tau}$.

This stability could, however, be improved by increasing the diode laser cavity's ζ . An enhanced cavity ζ laser could be made either by increasing the diode laser's facet reflectivity or by increasing the laser's length. In this case one would ultimately be limited by the ability to lock the diode laser frequency to an atomic absorption line. According to Shimoda,¹⁸ for a perfect photodetector and 3 milliwatts of diode laser power this limit is $\sigma_y^L(\tau) = 8.14 \times 10^{-15} / \sqrt{\tau}$ for a linear absorption technique.

As previously mentioned it is our intent to calculate the frequency stability of the atomic standard for various diode laser intensities. However, the partial derivative $\partial f/\partial v$ in Eq. (6) is evaluated at a fixed laser intensity. Fortunately, since $\partial f/\partial v$ is a linear function of the laser intensity, we have

$$\frac{\partial f}{\partial v} = \left(\frac{\partial^2 f}{\partial v \partial I} \right) I \quad (7)$$

and

$$\frac{\delta f}{f_o} = \left(\frac{v_o}{f_o} \right) \left(\frac{\partial^2 f}{\partial v \partial I} \right) \left(\frac{\delta v}{v_o} \right) I \quad (8)$$

where f_o and v_o are the 0-0 hyperfine transition frequency and the D_2 optical transition frequency, respectively. In terms of the Allan variance Eq. (8) becomes

$$\sigma_y^c(\tau) = \left(\frac{v_o}{f_o} \right) \left(\frac{\partial^2 f}{\partial v \partial I} \right) I \cdot \sigma_y^L(\tau) \quad (9)$$

where $\sigma_y^c(\tau)$ is the Allan variance of the clock's fractional frequency fluctuations due to laser frequency fluctuations. For 100 torr of nitrogen, using the theory of Mathur et al.,¹⁴ we calculate that $(v_o/f_o)(\partial^2 f/\partial v \partial I) = 0.68 \text{ cm}^2/\text{mW}$.

Atomic Standard Stability

From the preceding discussion it is apparent that in the present work we consider the atomic standard's frequency stability to result from two uncorrelated processes. The first is the shot noise at the atomic standard's photodetector; this is equivalent to the noise process that currently limits the short term frequency stability of gas cell atomic frequency standards. Additionally, there is the laser frequency noise which is transferred to the atomic standard via the light shift effect. If we write the clock's total white noise Allan variance as $\sigma_y(\tau) = \Lambda/\sqrt{\tau}$, then from Eq. (9) we have for Λ :

$$\Lambda^2 = a^2(I) + 0.46 \beta^2 I^2 \quad (10)$$

where $\sigma_y^L(\tau) = \beta/\sqrt{\tau}$

$$\beta = 9.02 \times 10^{-12} \text{ for current CSP diode lasers}$$
$$8.14 \times 10^{-15} \text{ for an enhanced cavity Q diode laser}$$

and where $a(I)$ is the atomic standard's shot noise limit coefficient for a laser intensity I computed by our non-empirical model of the gas cell atomic frequency standard as modified by the more realistic envelope function of Eq. (5). Parameters used in the present calculation are collected in Table I.

RESULTS

Figure 3 shows how the resonance cell temperatures and peak microwave Rabi frequencies that minimize the clock signal's shot noise Allan variance vary with diode laser intensity. Since the primary effect of a temperature increase in the model is to increase the rubidium number density, it is apparent from the figure that increasing laser intensities require increasing alkali vapor densities. To understand why this trend is physically reasonable, it is only necessary to realize that the signal-to-noise ratio of the clock goes roughly as $\Delta I/\sqrt{I_e}$, where ΔI is the change in transmitted laser intensity due to the microwaves and I_e is the laser intensity at the exit face of the resonance cell. If the incident laser intensity increases, then an increase in the alkali density can both increase ΔI and decrease I_e ; thus, there is a net increase in the signal to noise ratio. However, for ΔI to increase with increasing laser intensity and alkali number density (note that an increased alkali number density implies an increased spin exchange relaxation rate) there must be a concomitant increase in the peak microwave Rabi frequency. This can be understood by noting that the value of ΔI begins to saturate when microwave power broadening of the transition lineshape first sets in.

Figure 4a shows the minimum Allan variance that can be obtained in the standard clock configuration at a particular incident laser intensity, and Fig. 4b is a magnification of the region between .01 and 1 mW/cm². The three curves are for the cases where: 1) laser quantum noise, laser locking noise and clock signal shot noise all contribute to the frequency standard's stability (i.e., we assume a commercially available diode laser); 2) only laser locking noise and clock signal shot noise contribute to the frequency standard's stability (i.e., we assume an enhanced cavity Q diode laser); and 3) only clock signal shot noise influences the standard's stability. The minimum attainable Allan variances of the diode laser pumped rubidium gas cell atomic frequency standard for the three different cases are collected in Table II, as well as the corresponding resonance cell temperatures and peak microwave Rabi frequencies. The most important points to note from this figure are:

- 1) The best shot noise limited performance is obtained at relatively low incident laser intensities. Thus, there is no obvious advantage to operating a rubidium gas cell clock with a high power single-mode dye laser.
- 2) Whereas in presently available rubidium gas cell frequency standards the white noise Allan variance is limited by the clock signal's shot noise, the present calculations indicate that diode laser pumped rubidium gas cell frequency standards will ultimately be limited by the frequency stability of the laser; this noise is transferred to the atomic standard via the light shift effect.

SUMMARY

In the present study we have found that a diode laser pumped gas cell atomic frequency standard has the potential for orders of magnitude improvement over existing gas cell standards, if the diode laser frequency is well stabilized. In order to put these results in the proper perspective, Fig. 5 compares the best projected Allan variances for the diode laser pumped gas cell atomic frequency standard discussed in this paper with the proposed performance of the stored ^{201}Hg ion frequency standard;¹⁹ additionally, for reference the present performance of rubidium gas cell atomic frequency standards is shown.²⁰ Though any projection of frequency stability must be taken with a grain of skepticism, it is clear that there are many avenues for order of magnitude improvement in frequency standards, and that the diode laser pumped rubidium gas cell atomic frequency standard is a very attractive prospect.

REFERENCES

- 1) See for example: P. Cerez, G. Avila, E. de Clercq, M. de Labachellerie and M. Tetu, in Proceedings of the 38th Annual Frequency Control Symposium (IEEE, New York, 1984), pp. 452-457.
- 2) L. L. Lewis, M. Feldman and J. C. Bergquist, *J. Phys. (Paris)* 42, Colloque C8, Supplement au n° 12, C8-271 (1981).
- 3) E. de Clercq, M. de Labachellerie, G. Avila, P. Cerez and M. Tetu, *J. Phys. (Paris)* 45, 239 (1984).
- 4) M. Arditi, *Metrologia* 18, 59 (1982).
- 5) L. Lewis and M. Feldman, in Proceedings of the 35th Annual Frequency Control Symposium (Electronic Industries Association, Washington D. C., 1981), pp. 612-624; C. H. Volk, J. C. Campano and R. P. Frueholz, in Proceedings of the 13th Annual Precise Time and Time Interval (PTTI) Application and Planning Meeting, NASA Conference Publication 2220 (NASA, Greenbelt MD, 1981) pp. 631-640.
- 6) J. Vanier, R. Kunski, A. Brisson and P. Paulin, *J. Phys. (Paris)* 42, Colloque C8, supplement au n° 12, C8-139 (1981).
- 7) S. Pancharatnam, *J. Opt. Soc. Am.* 56, 1636 (1966); S. Pancharatnam, *Proc. R. Soc. Lond. A.* 330, 281 (1972).
- 8) J. C. Campano and R. P. Frueholz, to be published *J. Appl. Phys.*
- 9) J. C. Campano and R. P. Frueholz, *Phys. Rev. A* 31, 1440 (1985).
- 10) J. C. Campano and R. P. Frueholz, *Phys. Rev. A* 32, 1888 (1985).
- 11) R. P. Frueholz and J. C. Campano, *J. Appl. Phys.* 57, 704 (1985).
- 12) P. Minguzzi, F. Strumia and P. Violino, *Nuovo Cimento* 46B, 145 (1966).
- 13) F. A. Franz, *Phys. Rev. A* 6, 1921 (1972).
- 14) B. S. Mathur, H. Tang and W. Happer, *Phys. Rev.* 171, 11 (1968).
- 15) S. Ch'en and M. Takeo, *Rev. Mod. Phys.* 29, 20 (1957).
- 16) M. Ohtsu, H. Fukada, T. Tako and H. Tsuchida, *Jap J. Appl. Phys.* 22, 1157 (1983).

- 17) C. H. Henry, IEEE J. Quantum Electron. QE-18, 259 (1982).
- 18) K. Shimoda, Jap. J. Appl. Phys. 12, 1222 (1973).
- 19) D. J. Wineland, W. M. Itano, J. C. Bergquist and F. L. Walls, in Proceedings of the 35th Annual Frequency Control Symposium (Electronic Industries Association, Washington D. C., 1981) pp. 602-611.
- 20) T. J. Lynch and W. J. Riley, in Proceedings of the 15th Annual Precise Time and Time Interval (PTTI) Applications and Planning Meeting (National Technical Information Service, Springfield VA, 1984, ADA-149-163) pp. 269-279.

Table I: Parameters used in the calculation of the clock signal shot noise contribution to the diode laser pumped gas cell clock's white noise Allan variance.

Parameter	Value
Laser Linewidth	50 MHz
Nitrogen Pressure	100 torr
Photodetector Responsivity	0.5 amps/watt
Microwave Cavity	TE 111
Microwave Cavity Length	3.8 cm
Microwave Cavity Radius	1.35 cm

Table II: Best white noise Allan variances and the corresponding laser intensities, resonance cell temperatures and peak microwave Rabi frequencies for the three calculated cases: 1) clock signal shot noise plus laser quantum noise plus laser locking noise; 2) clock signal shot noise plus laser locking noise; 3) clock signal shot noise only.

Case No.	Laser Intensity	Cell Temp.	Rabi Frequency	Best $\sigma_y(\tau)$
1	$2.6 \mu\text{W}/\text{cm}^2$	47°C	17 Hz	$2.7 \times 10^{-14}/\sqrt{\tau}$
2	$120 \mu\text{W}/\text{cm}^2$	71°C	140 Hz	$5.5 \times 10^{-15}/\sqrt{\tau}$
3	$190 \mu\text{W}/\text{cm}^2$	74°C	170 Hz	$5.4 \times 10^{-15}/\sqrt{\tau}$

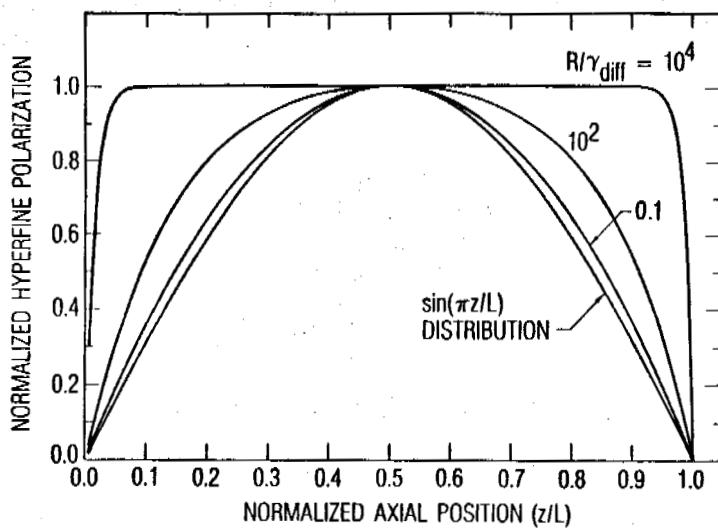


Figure 1: The envelope function $f(z)$ describing the spatial distribution of hyperfine polarization $\langle \vec{I} \cdot \vec{S} \rangle$ as a function of axial position within the resonance cell. The calculations assume that there is no collisional relaxation ($\gamma_1 = 0$). Several curves are shown corresponding to relative values of the photon absorption rate R (i.e., R/Y_{diff} where Y_{diff} is a diffusional relaxation rate). These curves are to be compared with the first order axial diffusion mode $\sin(\pi z/L)$.

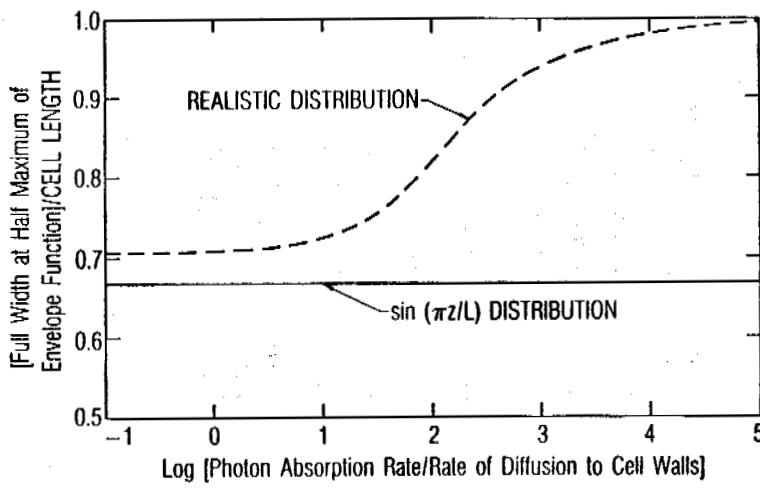


Figure 2: The full width at half maximum of the envelope function normalized to the resonance cell length as a function of the relative photon absorption rate. The true spatial distribution is always wider than what the first order diffusion mode would predict. However, when $R/Y_{\text{diff}} \gtrsim 100$, there is a significant broadening of the spatial distribution of hyperfine polarization such that analysis based on a first order diffusion mode approximation is in error.

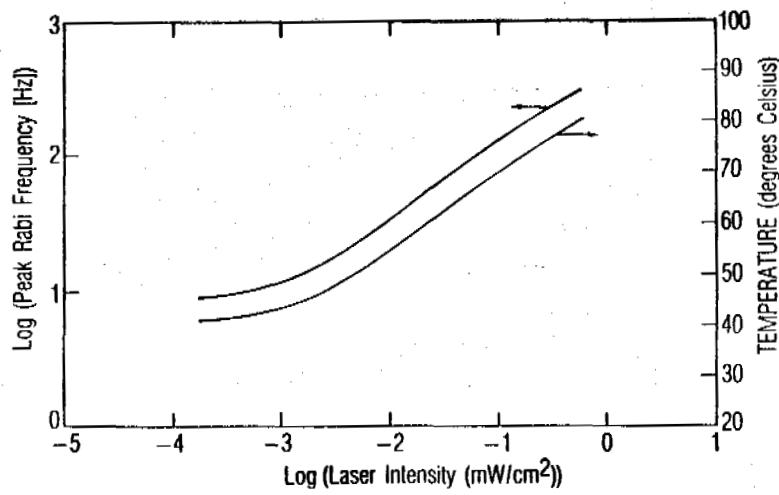


Figure 3: Using the non-empirical model of the gas cell atomic frequency standard, modified by the more appropriate envelope function discussed in the text, this figure shows the microwave Rabi frequencies and resonance cell temperatures that minimize the clock signals' shot noise Allan variance as a function of incident laser intensity.

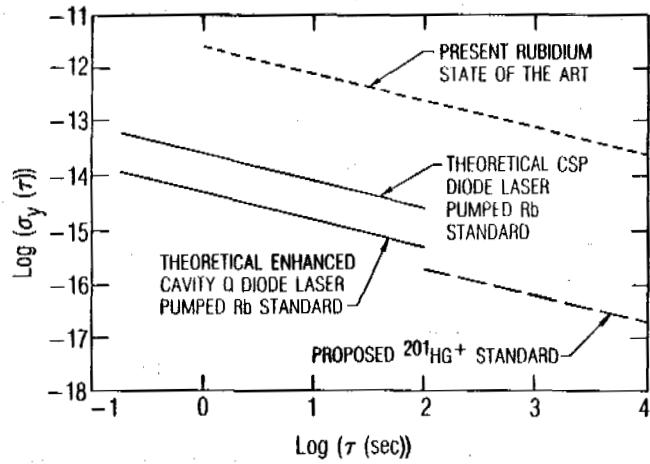


Figure 5: This figure is a comparison of diode laser pumped clocked performance with presently available rubidium standards and the proposed $^{201}\text{Hg}^+$ standard. It should be noted, however, that while the projected stabilities of the diode laser pumped gas cell clock and mercury ion standard are similar, the mercury ion standard as presently envisaged has the potential to be a primary standard.

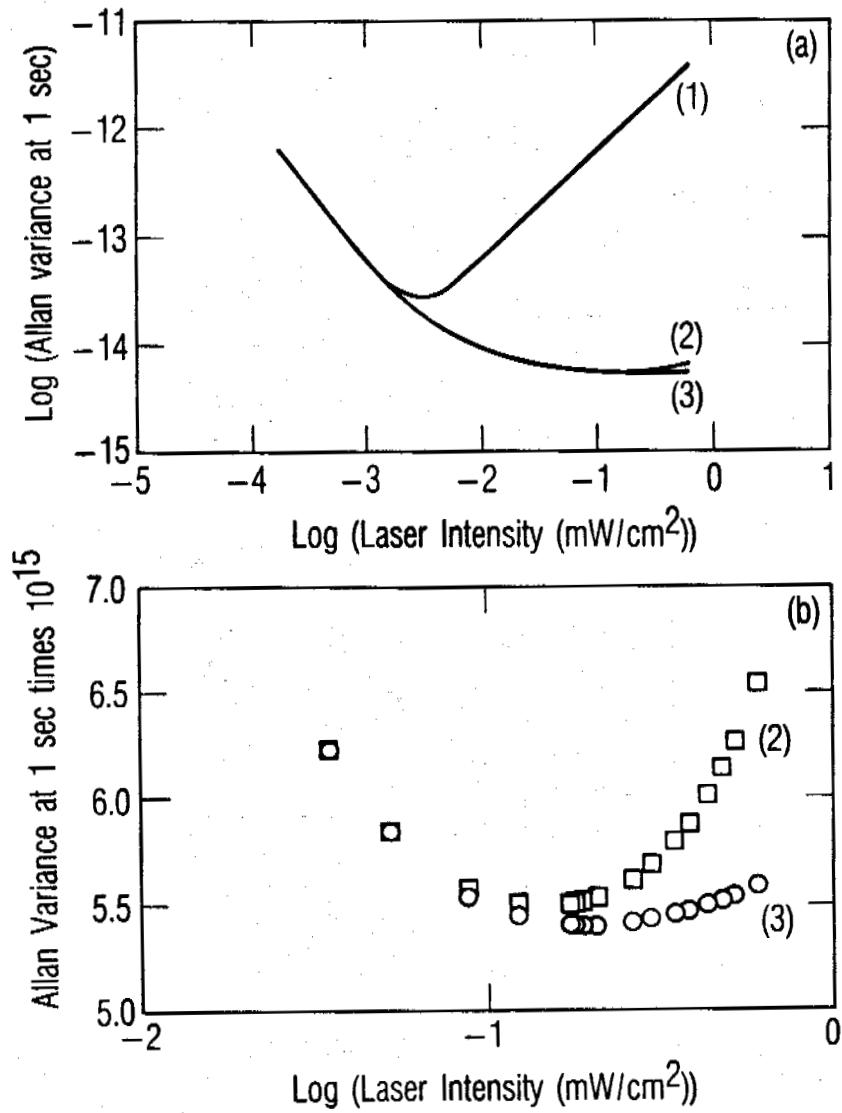


Figure 4: a) Curves 1, 2 and 3 illustrate the Allan variance at 1 second for a diode laser pumped Rb frequency standard with conditions (resonance cell temperature and microwave Rabi frequency) chosen in such a way that the clock signal's shot noise contribution is a minimum. Curve 1 assumes clock signal shot noise, diode laser quantum noise and diode laser frequency locking noise all contribute to the atomic clock's stability. Curve 2 assumes that only clock signal shot noise and diode laser frequency locking noise are important. Curve 3 shows the atomic clock's stability if only clock signal shot noise is present. Figure (b) is a magnification of Figure (a) in the region between 0.01 and 1 mW/cm².

QUESTIONS AND ANSWERS

UNIDENTIFIED QUESTIONER:

Do you have any plans to realize this diode pump?

MR.CAMPARO:

Not at the present time. This is basically a calculation that assumes that the experiment is done perfectly. There are a lot of systematic effects that could be a real problem. For one, there is optical feedback. In some of the work that we have done with optical pumping you can see the effect of optical feedback changing the frequency of the diode laser. It is drastic. If you have any optical feedback, and any mechanical instability associated with your apparatus that will lead to laser frequency fluctuations which have not been modeled. This could seriously degrade the performance that you would get as opposed to our calculations. The experiments will have some tricky problems that will have to be worked out that aren't considered in the calculations.

